Modelling of the Influence of Tensile Test Speed on the Fracture Load

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This investigation focuses on modelling the fracture zone of four materials at different test speeds. The influence of these test speeds on the fracture zone formula was investigated as well. The fracture behaviour of materials is an important parameter which greatly affects the performance of these materials. In this paper, an empirical formula was generated to predict the fracture zone. This formula was produced from experimental characterisation of the fracture process at different loading rates for some engineering materials. Statistical analysis was done for the results being obtained from the experimental work to verify the accuracy of this formula, and it was found that it can introduce an accurate base for fracture zone prediction and determination. It was noted that at fracture process initiation, there are no significant effects of varying loading rate; this effect is increased with increasing the fracture process propagation.

Keywords: tensile testing; fracture mechanics; loading rate; fracture zone; dynamic loading

I. INTRODUCTION

Engineering materials are classified in accordance to their deformation at fracture (i.e., brittle or ductile), to the form and appearance of fracture where ductile fracture produces less serious problems than brittle fracture under the same operating conditions, and to the crystallographic manner in which the fracture occurs (i.e., sliding, cleavage) (Hutiu *et al.*, 2018). Among the various failure mechanisms introduced (Fan *et al.*, 2017), investigating those associated with a brittle and ductile fracture in metallic alloys is important. Ductile fracture includes failure plastic instability or by cavitation.

Brittle fracture includes both intergranular fracture and cleavage. Recently developed advanced high-strength materials like advanced ceramics and nanocrystalline metallic materials, usual failure in a catastrophic brittle behaviour, which makes it urgent to determine a reasonable fracture criterion to predict their brittle fracture behaviours (Pineau *et al.*, 2016; Guptaab *et al.*, 2015). Though there are different models and rules for engineering metallic material

fracture, it makes many troubles for engineering application, because of lack of the reasonable description of fracture principle and change law (Qu and Zhang, 2013). The fracture resistance of many materials such as composite materials as well as some other metallic materials is increased by stiffening technique because shielding of the cracks ends by a nonlinear area of microcracking distribution or voids formalisation. In those materials, more careful definitions are required for the fracture energy, and the fracture behaviours of the sole material characteristic have not been represented (Carpinteri *et al.*, 2003).

The size of the nonlinear fracture process area at the cracks tips is another essential characteristic that needs to be investigated (Andrew Braham, 2016). It is required to determine the size of the fracture zone of microcracking or voids formation. It could be determined by the size of the inhomogeneities in material microstructure, and if the size of this fracture process zone is trivial in comparing with the structure dimensions or specimens, the fracture behaviour approaches that of linear elastic fracture mechanics. If the

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size of this zone includes all or most of the structure or specimen surface, the failure is determined by yield criterion or determination of the strength. If the size of this zone is moderate, the fracture behaviours are transitive between the linear elastic fracture mechanics and the strength criterion. This transitive behaviour which is important for many applications, and it was focused on it in this investigation.

The nonlinear fracture process area (fracture zone) gives relevant altitude to the size effect which might be explained by a rather simple size effect law recently proposed by Bazant (Qu and Zhang, 2013; Guo and Hu, 2013). It has been shown that this law can be utilised to determine the fracture energy of the material simply by the measurement of the maximum loads of geometrically similar specimens of sufficiently different sizes (Al-Maliky and Parry, 2004; Bazant and Kazem, 1990). In tensile testing the determination of the fracture zone is greatly affected by the testing machine force transducer's response time is an important parameter to be considered for practical applications. The typical force sensor behaviour is the same as an oscillated stiff spring, to achieve an accurate determination for the specified testing load value, the load transducer must achieve that is, stop oscillating - in less time than the required loading period (Bazant, 1985). For high-speed check loading (high loading rate of tensile testing) or rotary filling machine requires fast response force sensors. Such fast response force sensors inhibit their natural oscillating frequency when a force is applied to them. However, although, the force sensors do not remove vibrations applied to them from the outer sources, such as nearby equipment, so it is still needed to isolate the force sensors from damage the force sensors once when the season changes to correct for any temperature-caused such vibration sources (Bazant et al., 1987).

At a high loading rate, it is required to ensure that only the testing load is transmitted to each force sensor. Other loads values, such as environmental like, vibration, shock loading, large temperature changes, sudden loading and pressure differentials occurs when heavy material is dumped on the force sensor which is occurred at high loading rate, tending to greater forces than the system's rated capacity, and hence can generate errors in the force sensor signal which tends to inaccurate determination of the fracture point (Alves, 2000).

The principal objective of this paper is to determine the fracture zone and to generate an empirical mathematical model to detect this fracture process zone and to make a relation between the test speed and this zone.

II. METHODOLOGY

A. Testing Material Characterisation

Different testing materials were used for this investigation the mechanical properties of these materials can be summarised as follow:

Poly (methyl methacrylate) (PMMA): with the tensile strength of 48–76MPa, shear modulus, 1700MPa (dynamic, 25°C);

Copper: Copper alloy with a grade of C106/CW024A. The yield point is reported as either a 0.5% extension under load or as a 0.2 % offset;

Steel rode: St37 rods were used in this investigation in the form of dumb shape with the Yield strength of 235Mpa and Tensile Strength of 360 Mpa;

Aluminium: Aluminum 6061-T6 samples were used in this investigation with the Yield Strength of 276Mpa, 68.9Gpa Modulus of Elasticity, and 17 % Elongation.

B. Testing Apparatus and Setup

Data on the effect of strain rate on fracture point and tensile properties of materials is scarce due to data sampling rate difficulties (ISO 7500-1, 2018). For accurate determination of the fracture zone, there are two major critical issues to determine the fracture points at high loading rates tensile testing:

- Intense oscillation of the applied force deteriorates the quality of the stress-strain curve;
- Continues monitoring of the existing strain and force (dynamic force measuring amplifier) is not reliable and not accurate at high strain rates.

Due to these difficulties, the following apparatuses were used in this investigation;

 The fully computerised tensile testing machine is used to perform the required tests; this machine was classified as 0.5 accuracy class in accordance with (ISO 7500-1, 2018). This machine was provided by a high precision extensometer to measure the displacement (Figure 1).



Figure 1. 5kN Tensile testing machine

 A high-speed transient recorder and data acquisition system is the modular platform for fast measurements of mechanical parameters. A transient recorder, data recorder, and data acquisition system provide all the features expected from a transient recorder. Genesis High Speed is provided with data acquisition cards with sampling rates of 20KS/s to 100MS/s. This modular platform (interfaced with 5kN dynamic force transducer) was used to monitor the testing force utilising the fast sampling rate to monitor the behaviour of the tested material from the force point of view (Figure 2).



Figure 2. High-Speed Recorder

 Dynamic Load Cell: for measurement of tensile dynamic force, this force transducer is suitable for very fast measurements. The capacity of this force transducer is 5kN with an accuracy class of 0.5 (Figure 3).

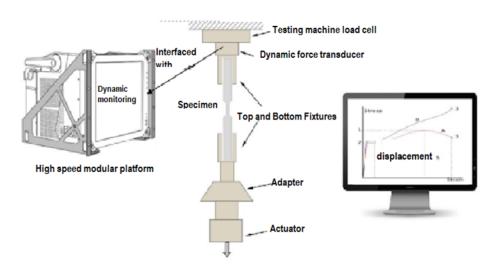


Figure 3. Setup of the measuring system

C. Test Procedure

Three machine speeds (5, 10 and 20) mm/min were used to test 3 samples per each rate for the selected materials. The

samples were prepared to fit the machine grips in tension mode. The top of the upper grip was assembled to the dynamic force transducer used. Warming up time for the equipment and the stability of the environmental conditions before and during the tests were observed. The dynamic force transducer interfaced with the modular platform for force/time fast measurement. Results were analysed, and force rate versus failure time curves was monitored. The fracture point is similar to applying inverse step force function on both the testing machine (force transducer and measuring amplifier) and the material under test.

Therefore, in this investigation, the fracture point was enlarged to present the fracture zone. In order to specify this fracture zone, the fracture yield point of each test curve (force-time) was picked, then move downwards for a constant time (specifically 571ms). To have a clear trend line for the results before the fracture point, all test measurements, for all tested materials, were checked and found that the 571ms

is adequate for all materials to be the start point of this fracture zone. The zero-force is considered the end of the fracture zone. To unify the representation of the fracture zone results for all the tested materials, the force value at the start point of the fracture zone is considered zero force and the subsequent forces were subtracted from its actual value.

III. RESULTS AND DISCUSSION

Figure 4 shows the fracture zone of the steel materials for the three different machine speeds as a sample from the four tested materials. It was shown that before and after the fracture yield point, there are two approximately straight lines; the line before has a specific decay and the line after has great decay to reach the zero force. The results of the fracture zone give the fracture curve as a force-time relation.

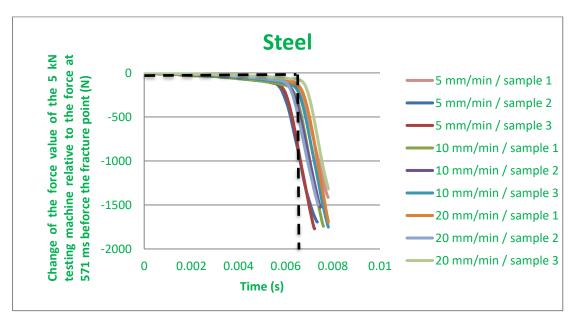


Figure 4. Fracture zone of steel (st37)

From Figure 4 and 5, it was noted that at fracture curve initiation there are no significant effects of varying loading rate, this effect is increased with increasing the fracture process propagation, at high loading rate the fracture zones can be extended more than estimated from low loading rate.

To generate the empirical formula to predict the fracture zone, statistical analysis was done for the results being obtained from the experimental work, and regression coefficients were calculated to estimate the relationship between a set of independent variables and some dependent variables. Different exponential functions are used to fit the results obtained from the experiments; the best fit exponential function is giving below.

$$y = A \times exp(R_0 \times x) \tag{1}$$

Where:

x: time (s)

y: force value (N)

A: initial force value (N)

Ro: force loading rate (N/s)

The adjusted R-square is the best estimate of the degree of relationship in the basic population. Table 1 shows the values of the coefficients from Equation 1 and the corresponding R-squares. The results of R- squares shown to give a quite fair degree of relationship.

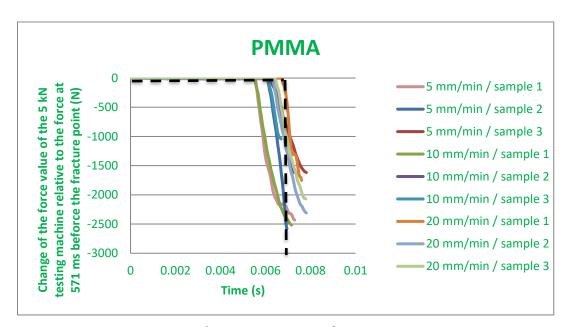


Figure 5. Fracture zone of PMMA

Table 1. Coefficients of the fracture zone fracture zone

Material	Machine loading rate	Sample	$y = A \times ex$	Adj. R-squares	
	(mm/min)		A	$R_{\rm o}$	R ²
		1	-0.02093	1442.341	0.97944
	5	2	-0.34616	1181.635	0.97407
		3	-0.07916	1403.714	0.98197
		1	-0.04773	1398.534	0.97917
Steel	10	2	-0.03295	1453.886	0.98142
		3	-0.04182	1379.933	0.98146
		1	-0.01860	1462.218	0.98209
	20	2	-0.02658	1501.308	0.97970
		3	-0.01384	1459.114	0.94045
PMMA		1	-0.00310	2110.625	0.94045
	5	2	-0.00002	2742.651	0.98023
		3	-0.01030	1590.721	0.95096
	10	1	-0.45706	1255.539	0.93202
		2	-0.00012	2286.211	0.97808
		3	0.00000	4522.782	0.96944
	20	1	0.00000	4701.334	0.96078
		2	-0.17080	1243.449	0.93494

		3	-0.03285	1449.617	0.93746
	5	1	-0.33317	880.4972	0.99326
		2	-0.02598	913.2547	0.99298
		3	-0.44783	941.8274	0.99528
	10	1	-0.11355	1201.796	0.98374
Aluminum		2	-0.93258	1109.256	0.98793
		3	-0.12144	1225.69	0.99463
	20	1	-1.02435	661.917	0.99800
		2	-0.08579	1230.387	0.98871
		3	-0.17526	869.6915	0.99054
Copper	5	1	-2.16403	968.7012	0.99069
		2	-10.3246	688.1021	0.99253
		3	-3.7452	547.9225	0.99479
	10	1	-1.59422	1010.312	0.99158
		2	-1.68862	658.3257	0.99137
		3	-0.04220	1399.423	0.98169
	20	1	-1.72506	1015.967	0.99192
		2	-1.36584	871.211	0.99371
		3	-2.5125	599.964	0.99606

To estimate the contribution of data sets of experimental measurements, the significance of each measurement on the mean value of each measurement group, for the two coefficients A and R_0 , is calculated as follows:

Significance of A or
$$R_0$$
 (S_i)= mean – value (2)

This significance (S_i) will be used to calculate the weighted mean of the coefficients A (symbol a) and R_0 (symbol b) as follows:

$$a = \sum \frac{A_i}{S_i^2} \tag{3}$$

$$b = \sum \frac{R_{0i}}{S_i^2} \tag{4}$$

The weighted uncertainties of these two weighted means are calculated as follows, in order to improve the confidence in the formula obtained (confidence level at 95% and coverage factor of k=2):

$$u_{aorb} = \sqrt{\frac{1}{\sum_{s_i^2}^{1}}}$$
 (5)

Table 2 shows the weighted means, and the corresponding uncertainties of the coefficients A and R_0 resulted from Equations 2 to 5. Table 2 shows that the weighted mean at different speeds, of the four selected materials, are different for both coefficients (A and R_0) which reflects the effect of the machine speed on the fracture zone. The calculated weighted uncertainties of the coefficients A and R_0 considered fair as a result of the tensile test.

Figures 6 to 9 show the graphical representation of the results of the coefficient *A*. For the ductile materials, steel, aluminium and copper, the values of *A* at machine speed 5mm/min has a certain value then decreased, regardless of the sign, to reach a stable level from speed 10mm/min to 20mm/min, on the other hand, for the brittle material, PMMA, it has opposite behaviour. At machine speed 5mm/min has a certain value then increased, regardless of the sign, to reach a stable level from speed 10mm/min to 20mm/min.

Table 2. The weighted means and the corresponding uncertainties of the coefficients A and R_0

Material	Machin e speed mm/mi n	Mean	Significanc e (S_i)	Weighted mean (a)	Weighted uncertainty (u _a)	Mean	Significanc e (S_i)	Weighted mean (b)	Weighted uncertaint $y(u_b)$
Steel	5	- 0.1488	0.1278 0.1974 0.0696	-0.0904	0.0584	1342.563 1	99.7775 160.9281 61.1506	- 1392.162 8	49.5997
	10	- 0.040 8	0.0069 0.0079 0.0010	-0.0418	0.0010	1410.784 3	12.2503 43.1012 30.8509	- 1399.776 - 4	11.0080
	20	- 0.0197	0.0011 0.0069 0.0058	-0.0186	0.0010	1474.213 3	11.9953 27.0943 15.0990	- 1465.339 2	8.8741
	5	- 0.0045	0.0014 0.0045 0.0058	-0.0032	0.0013	2147.999 0	37·3737 594.6521 557·2784	- 2110.782 1	37.2169
PMMA	10	- 0.1524	0.3047 0.1523 0.1524	-0.0508	0.1016	2688.177 0	1432.6383 401.9662 1834.6045	- 2309.49 06	378.6864
	20	- 0.0679	0.0679 0.1029 0.0350	-0.0381	0.0298	2464.80 00	2236.5340 1221.3512 1015.1827	1727.7115	737.0885
	5	- 0.2690	0.0642 0.2430 0.1788	-0.3276	0.0586	911.8598	31.3626 1.3949 29.9676	913.2518	1.3921
Alumini um	10	- 0.3892	0.2756 0.5434 0.2678	-0.2081	0.1811	1178.913 8	22.8821 69.6583 46.7761	· 1198.628 0	19.7142
	20	- 0.4285	0.5959 0.3427 0.2532	-0.2358	0.1927	920.6652	258.7482 309.7218 50.9737	871.2923	49.3729
Copper	5	-3.7154	0.9133 0.3339	-3.7154	0.3042	734.9086	233.7926 46.8065 186.9861	690.3359	44.5727

10	-1.1083	0.4859 0.5803 1.0661	-1.4600	0.3517	1022.686	12.3752 364.3612 376.7364	1010.325 5	12.3614
20	- 1.8678	0.1427 0.5020 0.6447	-1.7335	0.1343	829.0472	186.9195 42.1638 229.0832	869.5302	40.4830

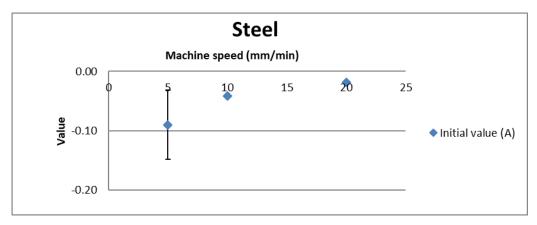


Figure 6. The initial value of the equation versus different loading rate for steel

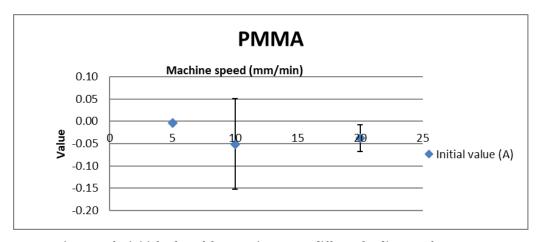


Figure 7. The initial value of the equation versus different loading rate for PMMA

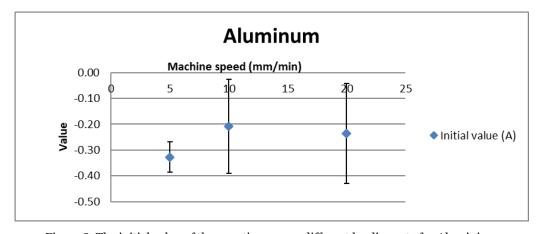


Figure 8. The initial value of the equation versus different loading rate for Aluminium

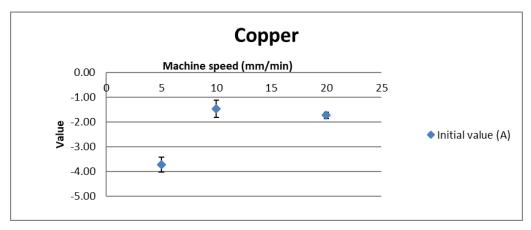


Figure 9. The initial value of the equation versus different loading rate for Copper

Figures 10 to 13 show the graphical representation of the results of the coefficient R_0 . Two of the ductile materials, aluminium, and copper, with the brittle material, PMMA, have a certain value of R_0 at machine speed 5mm/min then

increased at 10mm/min and then decreased at 20mm/min. Only the steel starts at a certain value at 5mm/min and still stable at 10mm/min then increased at 20mm/min.

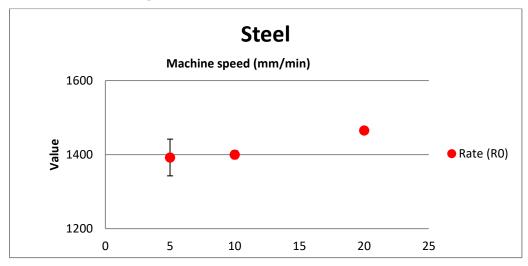


Figure 10. Loading rate value of the equation versus the fracture force for Steel

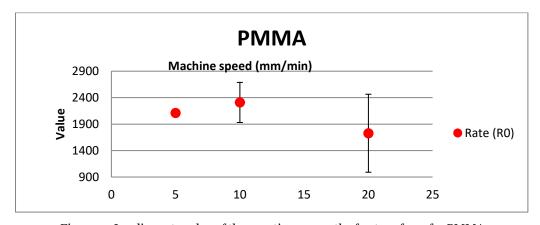


Figure 11. Loading rate value of the equation versus the fracture force for PMMA

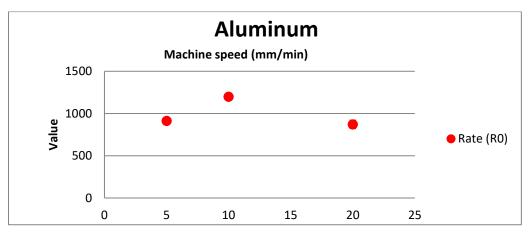


Figure 12. Loading rate value of the equation versus the fracture force for Aluminium

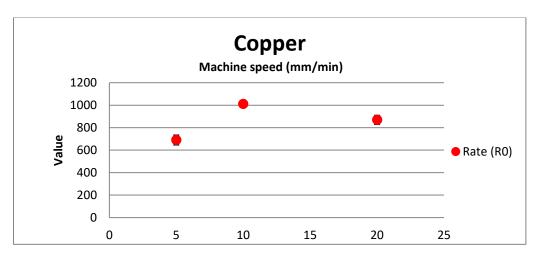


Figure 13. Loading rate value of the equation versus the fracture force for Copper

From the previous Figures (11 to 13), it was noted that test loading rate effect for ductile materials is behaving, in a similar manner, differing from that of quasi-brittle and the fracture mechanical behaviour of quasi-brittle materials is different from ductile materials, where cracks growth in ductile materials due to the intersections and coalescences of micro-void, while in quasi-brittle materials such as PMMA, crack propagation when the aggregates interlock or when micro-crack bridging occurs.

IV. CONCLUSION

From this investigation, it was concluded that:

 Modelling of tension fracture and cracking in engineering and composite materials is an important issue to improve the load-bearing capacity and reliability of these materials. In this study, experimental work is used to model the fracture zone and to investigate the effects of loading rate. An empirical model was produced to correlate the fracture load with the loading rate and to predict and accurate determination of the fracture zone. This model improves the determination and analysis of fracture force prediction and is more accurate than other developed models.

- Test loading rate effect for ductile materials is behaving, in similar manner, differing from that of quasi-brittle and The fracture mechanical behaviour of ductile materials is different from that of quasi-brittle materials, where cracks growth in ductile materials due to the coalescences and intersections of micro-void, while in quasi-brittle materials such as PMMA, cracks propagate when the aggregates interlock or when micro-crack bridging occurs
- The difference of the material behaviour under dynamic and quasi-static loading is that the dynamic strength or yield stress increases as the strain rate increases.

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